

# Stability Analysis Of Uncertain Neutral-Type Systems

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**Abstract**—This paper studies the problem of the stability analysis for uncertain neutral-type systems. By constructing an appropriate Lyapunov-Krasovskii functional, some new delay-dependent criteria can be obtained by using the free-weighting matrices approach to estimate the derivative of the Lyapunov functional, which are established in terms of linear matrix inequalities (LMIs). The novelties in this paper are that any bounding technique and any mode transformation method are not utilized. Finally, a numerical example is presented to illustrate the effectiveness of the proposed method.

**Keywords**— Stability analysis, Neutral systems, Lyapunov method, Linear Matrix Inequality

## I. INTRODUCTION

Time delays are frequently encountered in many practical engineering systems, such as chemical processes, long transmission lines in pneumatic systems [1]-[8]. It has been shown that the presence of a time delay in a dynamical system is often a primary source of instability and performance degradation [9]. Delay-dependent robust stability criteria of uncertain fuzzy systems with state and input delays are presented in [10]. Dynamical systems with distributed time-varying delays have been of considerable interest for the fast few decades. In particular, the interest in stability analysis of various delay differential systems has been growing rapidly due to their successful applications in practical fields such as circuit theory, aircraft stabilization, population dynamics, distributed networks, manual control and so on. Current efforts on the problem of stability of distributed time-varying delays system can be divided into two categories, namely delay independent criteria and delay dependent criteria. Distributed delay systems have been considered in [11]-[28].

The issue of stability for uncertain neutral systems using Linear Matrix Inequalities (LMI) approach is studied in this paper. We established a new LMI condition by using the Lyapunov-Krasovskii functional to guarantee the asymptotic stability of the system concerned. A sufficient condition for the solvability of this problem is proposed in terms of Linear Matrix Inequalities (LMIs) and the validity of this result is checked numerically using the effective LMI control toolbox in MATLAB.

NOTATIONS: Throughout this paper, for a matrix  $B$  and two symmetric matrices  $A$  and  $C$ ,

$$\begin{bmatrix} A & B \\ & C \end{bmatrix}$$

denote the symmetric matrix, where the notation  $*$  represents the entries implied by symmetry.  $A^T$  and  $A^{-1}$  are denotes the matrix transpose and inverse of  $A$  respectively. We say  $X > 0$  for  $X \in \mathfrak{R}^n$  means that the matrix  $X$  is real symmetric positive definite.  $\|P\|$  refers to the Euclidean norm for vectors. And  $I$  denotes the identity matrix with appropriate dimensions.

## II. PROBLEM FORMULATION AND MAIN RESULTS

Consider the following uncertain Neutral-type neural networks with discrete and distributed delay.

$$\begin{cases} \dot{x}(t) = -A(t)x(t) + W_0(t)f(x(t)) + W_1(t)f(x(t-\tau)) + Cx(t-\tau) \\ x(\theta) = \phi(\theta), \forall \theta \in [-\eta, 0], \eta = \max\{h, \tau, r\} \end{cases} \quad (1)$$

Where  $x(t) \in R^n$  is the state vector.  $h, \tau, t$  represent the neutral-delay, discrete delay and distributed-delay, respectively. The initial condition  $\phi(t)$  denotes a continuous vector-valued initial function on the interval  $[-\eta, 0]$ .  $A, W_0, W_1, C$  and  $W_2 \in R^{n \times n}$  are constant matrices, For system (1), the nominal form is given as follows:

$$\begin{cases} \dot{x}(t) = -Ax(t) + W_0f(x(t)) + W_1f(x(t-\tau)) + Cx(t-\tau) \\ x(\theta) = \phi(\theta), \forall \theta \in [-\eta, 0], \eta = \max\{h, \tau, r\}. \end{cases} \quad (2)$$

## III. MAIN RESULTS

**Theorem 3.1** For three given scalars  $h > 0, \tau > 0,$  and  $r > 0,$  if there exist some positive definite symmetric matrices:  $P_{11}, P_{22}, P_{33}, P_{44}, Q_i (i = 1, 2, \dots, 8) \in R^{n \times n}$  and some appropriately dimensional matrices:  $(P_{ij})_{1 \leq i < j \leq 4}, K = [K_1^T, K_2^T]^T, L = [L_1^T, L_2^T]^T, M = [M_1^T, M_2^T]^T, N = [N_1^T, N_2^T]^T,$  such that the following linear matrix inequalities (LMIS) hold.

$$P = \begin{bmatrix} P_{11} & P_{12} & P_{13} & P_{14} \\ * & P_{22} & P_{23} & P_{24} \\ * & * & P_{33} & P_{34} \\ * & * & * & P_{44} \end{bmatrix} \geq 0, \quad (3)$$

and

$$\Xi^1 < 0, \quad (4)$$

$$\Xi^2 < 0,$$

Where,

$$\Xi^k = (\Omega_{ij}^k)_{9 \times 9},$$

$$\Omega_{11}^k = [-P_{11}A - A^T P_{11}^T + P_{13}^T + P_{13} + P_{14}^T + P_{14} - Q_1 + Q_3 + hQ_4 + \tau Q_5 + K_1^T + K_1 + hL_1^T + hL_1 + M_1 + M_1^T + \tau N_1^T + \tau N_1],$$

$$\Omega_{12}^k = [-A^T P_{12} + P_{23}^T - P_{13} + P_{24}^T - K_1^T + K_2 + hL_2], \quad \Omega_{13}^k = [P_{12} + P_{11}C],$$

$$\Omega_{14}^k = [-P_{14} - M_1^T + M_2 + \tau N_2], \quad \Omega_{15}^k = P_{11}W_0, \quad \Omega_{16}^k = P_{11}W_1,$$

$$\Omega_{17}^k = P_{11}W_2, \quad \Omega_{18}^1 = h[-A^T P_{13} + P_{33} + P_{34}^T - L_1^T],$$

$$\Omega_{18}^2 = \tau[-A^T P_{14} + P_{34} + P_{44}^T - N_1^T], \quad \Omega_{19}^1 = -hk_1^T - \frac{h^2}{2} L_1^T, \quad \Omega_{19}^2 = -\tau M_1^T - \frac{\tau^2}{2} N_1^T,$$

$$\Omega_{22}^k = [-P_{23}^T - P_{23} - K_2^T - K_1 - Q_1], \quad \Omega_{23}^k = [P_{22} + P_{12}^T C], \quad \Omega_{24}^k = [-P_{24}],$$

$$\Omega_{25}^k = [P_{12}^T W_0], \quad \Omega_{26}^k = [P_{12}^T W_1], \quad \Omega_{27}^k = [P_{12}^T W_2], \quad \Omega_{28}^1 = h[-P_{33} - L_2^T],$$

$$\Omega_{28}^2 = \tau P_{34}, \quad \Omega_{29}^1 = -hk_2^T - \frac{h^2}{2} L_2^T, \quad \Omega_{29}^2 = 0, \quad \Omega_{33}^k = -Q_2, \quad \Omega_{34}^k = 0,$$

$$\Omega_{35}^k = 0, \quad \Omega_{36}^k = 0, \quad \Omega_{37}^k = 0, \quad \Omega_{38}^1 = h[C^T P_{13} + P_{23}],$$

$$\Omega_{38}^2 = \tau[C^T P_{14} + P_{24}], \quad \Omega_{39}^k = 0, \quad \Omega_{44}^k = [-Q_3 - M_2^T - M_2], \quad \Omega_{45}^k = 0, \quad \Omega_{46}^k = 0, \quad \Omega_{47}^k = 0,$$

$$\Omega_{48}^1 = h[-P_{34}], \quad \Omega_{48}^2 = \tau[-P_{44}^T - N_2^T], \quad \Omega_{49}^1 = 0, \quad \Omega_{49}^2 = -\tau M_2^T - \frac{\tau^2}{2} N_2^T,$$

$$\Omega_{55}^k = [r^2 Q_8 + S], \quad \Omega_{56}^k = 0, \quad \Omega_{57}^k = 0, \quad \Omega_{58}^1 = h[W_0^T P_{13}], \quad \Omega_{58}^2 = \tau[W_0^T P_{14}],$$

$$\Omega_{59}^k = 0, \quad \Omega_{66}^k = [-S], \quad \Omega_{67}^k = 0, \quad \Omega_{68}^1 = h[W_1^T P_{13}], \quad \Omega_{68}^2 = \tau[W_1^T P_{14}], \quad \Omega_{69}^k = 0,$$

$$\Omega_{77}^k = [-Q_8], \quad \Omega_{78}^1 = h[W_2^T P_{13}], \quad \Omega_{78}^2 = \tau[W_2^T P_{14}], \quad \Omega_{79}^k = 0, \quad \Omega_{88}^1 = [-hQ_4],$$

$$\Omega_{88}^2 = [-\tau Q_5], \quad \Omega_{89}^k = 0, \quad \Omega_{99}^1 = [-hQ_6 - \frac{h^2}{2} Q_9], \quad \Omega_{99}^2 = [-\tau Q_7 - \frac{\tau^2}{2} Q_{10}],$$

and \* means the symmetric terms, then the nominal system (4) is asymptotically stable.

**Proof:** Define a Lyapunov-krasovskii functional candidate for system (4) as

$$V(t, x) = V_1(t, x) + V_2(t, x) + V_3(t, x), \quad (6)$$

Where

$$V_1(t, x) = \xi^T(t) P \xi(t),$$

$$\begin{aligned}
 V_2(t, x) &= \int_{t-h}^t x^T(s)Q_1x(s)ds + \int_{t-h}^t \dot{x}^T(s)Q_2\dot{x}(s)ds \\
 &+ \int_{t-\tau}^t x^T(s)Q_3x(s)ds + \int_{t-\tau}^t f^T(x(s))Sf(x(s))ds, \\
 V_3(t, x) &= \int_{-h}^0 \int_{t+\theta}^t x^T(s)Q_4x(s)dsd\theta + \int_{-\tau}^0 \int_{t+\theta}^t x^T(s)Q_5x(s)dsd\theta \\
 &+ \int_{-h}^0 \int_{t+\theta}^t \dot{x}^T(s)Q_6\dot{x}(s)dsd\theta + \int_{-\tau}^0 \int_{t+\theta}^t \dot{x}(s)Q_7\dot{x}(s)dsd\theta \\
 &+ r \int_{-\tau}^0 \int_{t+\theta}^t f^T(x(s))Q_8f(x(s))dsd\theta
 \end{aligned}$$

Where

$$\xi(t) = \begin{bmatrix} x^T(t) & x^T(t-h) & \int_{t-h}^t x^T(s)ds & \int_{t-\tau}^t x^T(s)ds \end{bmatrix}.$$

Then, the time derivative of  $V(t, x)$  with respect to  $t$  along the system (4) is .

$$\dot{V}(t, x) = \dot{V}_1(t, x) + \dot{V}_2(t, x) + \dot{V}_3(t, x), \tag{7}$$

Where

$$\begin{aligned}
 \dot{V}_1(t, x) &= 2[x^T(t)P_{11} + x^T(t-h)P_{12}^T + \int_{t-h}^t x^T(s)dsP_{13}^T + \int_{t-\tau}^t x^T(s)dsP_{14}^T] \\
 &[-Ax(t) + W_0f(x(t)) + W_1f(x(t-\tau)) + C\dot{x}(t-h) + W_2 \int_{t-\tau}^t f(x(s))ds] \\
 &+ 2[x^T(t)P_{12} + x^T(t-h)P_{22} + \int_{t-h}^t x^T(s)dsP_{23}^T + \int_{t-\tau}^t x^T(s)dsP_{24}^T]\dot{x}(t-h) \\
 &+ 2[x^T(t)P_{13} + x^T(t-h)P_{23} + \int_{t-h}^t x^T(s)dsP_{33} + \int_{t-\tau}^t x^T(s)dsP_{34}^T][x(t) - x(t-h)] \\
 &+ 2[x^T(t)P_{14} + x^T(t-h)P_{24} + \int_{t-h}^t x^T(s)dsP_{34} + \int_{t-\tau}^t x^T(s)dsP_{44}][x(t) - x(t-\tau)], \tag{8}
 \end{aligned}$$

$$\begin{aligned}
 \dot{V}_2(t, x) &= x^T(t)[Q_1 + Q_3]x(t) + x^T(t-h)[-Q_1]x(t-h) + \dot{x}^T(t)[Q_2]\dot{x}(t) \\
 &+ \dot{x}^T(t-h)[-Q_2]\dot{x}(t-h) + x^T(t-\tau)[-Q_3]x(t-\tau) \\
 &+ f^T(x(t-\tau))[-S]f(x(t-\tau)) + f^T(x(t))[S]f(x(t)), \tag{9}
 \end{aligned}$$

$$\begin{aligned}
 \dot{V}_3(t, x) &= x^T(t)[hQ_4 + \tau Q_5]x(t) + f^T(x(t))[r^2Q_8]f(x(s)) \\
 &+ \dot{x}^T(t)[hQ_6 + \tau Q_7]\dot{x}(t) \\
 &- \int_{t-h}^t \dot{x}^T(s)[Q_4]x(s)ds - \int_{t-\tau}^t x^T(s)[Q_5]x(s)ds - \int_{t-h}^t \dot{x}^T(s)[Q_6]\dot{x}(s)ds
 \end{aligned}$$

$$-\int_{t-\tau}^t \dot{x}^T(s)[Q_7]\dot{x}(s)ds - r \int_{t-r}^t f^T(x(s))[Q_8]f(x(s))ds. \tag{10}$$

By using the Jensen`s inequality

$$[\int_0^r w(s)ds]^T M [\int_0^r w(s)ds] \leq r \int_0^r w^T(s)Mw(s)ds$$

We have,

$$\begin{aligned} \dot{V}_3(t, x) &= x^T(t)[hQ_4 + \tau Q_5]x(t) + f^T(x(t))[r^2 Q_8]f(x(t)) \\ &+ \dot{x}^T(t)[hQ_6 + \tau Q_7]\dot{x}(t) \\ &- [\int_{t-h}^t x(s)ds]^T [Q_4]x(s) - [\int_{t-\tau}^t x(s)ds]^T [Q_5]x(s) - [\int_{t-h}^t \dot{x}(s)ds]^T [Q_6]\dot{x}(s) \\ &- [\int_{t-\tau}^t \dot{x}(s)ds]^T [Q_7]\dot{x}(s) - [\int_{t-r}^t f(x(s))ds]^T [Q_8][\int_{t-r}^t f(x(s))ds]. \end{aligned} \tag{11}$$

And from Leibinz-Newton Formula the following appropriate dimension, equating are true for real matrices  $K, L, M, N$  with an

$$\alpha_1(t) := 2\xi_1^T(t)K^T[x(t) - x(t-h) - \int_{t-h}^t \dot{x}(s)ds] = 0, \tag{12}$$

$$\alpha_2(t) := 2\xi_1^T(t)L^T[hx(t) - \int_{t-h}^t x(s)ds - \int_{-h}^0 \dot{x}(s)dsd\theta] = 0, \tag{13}$$

$$\alpha_3(t) := 2\xi_2^T(t)M^T[x(t) - x(t-\tau) - \int_{t-\tau}^t \dot{x}(s)] = 0, \tag{14}$$

Where

$$\xi_1(t) = \begin{bmatrix} x^T(t) & x^T(t-h) \end{bmatrix}^T, \xi_2(t) = \begin{bmatrix} x^T(t) & x^T(t-\tau) \end{bmatrix}^T.$$

Suppose that

$$\begin{aligned} \sum_{i=1}^4 \alpha_i(t) &= x^T(t)[K_1^T + K_1 + hL_1^T + hL_1 + M_1^T + M_1]x(t) \\ &+ 2x^T(t)[-K_1^T + K_2 + hL_2]x(t-h) + 2x^T(t)[-M_1^T + M_2]x(t-\tau) \\ &+ x^T(t-h)[-K_2^T - K_2]x(t-h) + x^T(t-\tau)[-M_2^T - M_2]x(t-\tau) \\ &+ x^T(t)[-hL_1^T]x(s) + 2x^T(t)[-hK_1^T - \frac{h^2}{2}L_1^T]\dot{x}(s) \\ &+ x^T(t) - \tau M_1^T \dot{x}(s) \\ &+ 2x^T(t-h)[-hL_1^T]x(s) \\ &+ 2x^T(t-h)[-hK_2^T - \frac{h^2}{2}L_2^T]\dot{x}(s) + 2x^T(t-\tau)[-M_2^T]\dot{x}(s). \end{aligned} \tag{15}$$

Combining from (10) to (15), we obtain

$$\dot{V}(t, x) = \dot{V}_1(t, x) + \dot{V}_2(t, x) + \dot{V}_3(t, x) + \sum_{i=1}^4 \alpha_i(t),$$

$$\begin{aligned}
\dot{V}(t, x) \leq & x^T(t)[-P_{11}^T A - P_{11} A^T + P_{13}^T + P_{13} + P_{14} + Q_1 + Q_3 + hQ_4 + \tau Q_5 + K_1^T + K_1 \\
& + hL_1^T + hL_1 + M_1^T + M_1]x(t) \\
& + 2x^T(t)[-A^T P_{12} + P_{23}^T - P_{13} + P_{24}^T - K_1^T + K_2 + hL_2]x(t-h) \\
& + 2x^T(t)[P_{12} + P_{11}C]\dot{x}(t-h) + 2x^T(t)[-P_{14} - M_1^T + M_2]x(t-\tau) \\
& + 2x^T(t)[P_{11}W_0]f(x(t)) + 2x^T(t)[P_{11}W_1]f(x(t-\tau)) \\
& + 2x^T(t)[P_{11}W_2]\int_{t-r}^t f(x(s))ds + 2x^T(t)h[-A^T P_{13} + P_{33}^T + P_{34}^T - L_1^T]x(s) \\
& + 2x^T(t)\tau[-A^T P_{14} + P_{34}^T + P_{44}^T]x(s) \\
& + 2x^T[-hK_1^T - \frac{h^2}{2}L_1^T]\dot{x}(s) + 2x^T(t)[- \tau M_1^T]\dot{x}(s) \\
& + 2x^T(t-h)[-P_{23}^T - P_{23} - K_2^T - K_1 - Q_1]x(t-h) \\
& + 2x^T(t-h)[P_{22} + P_{12}^T C]\dot{x}(t-h) + 2x^T(t-h)[P_{24}]x(t-\tau) \\
& + 2x^T(t-h)[P_{12}^T W_0]f(x(t)) + 2x^T(t-h)[P_{12}^T W_1]f(x(t-\tau)) \\
& + 2x^T(t-h)[P_{12}^T W_2]\int_{t-r}^t f(x(s))ds \\
& + 2x^T(t-h)h[-P_{33} - L_1^T]x(s) + 2x^T(t-h)[\tau P_{34}]x(s) \\
& + 2x^T(t-h)[-hK_2^T - \frac{h^2}{2}L_2^T]\dot{x}(s) + 2\dot{x}^T(t-h)[-Q_2]\dot{x}(t-h) \\
& + 2\dot{x}^T(t-h)h[C^T P_{13} + P_{23}]x(s) + 2\dot{x}^T(t-h)\tau[C^T P_{14} + P_{24}]x(s) \\
& + x^T(t-\tau)[-Q_3 - M_2^T - M_2]x(t-\tau) \\
& + 2x^T(t-\tau)h[-P_{34}^T]x(s) + 2x^T(t-\tau)\tau[-P_{44}^T - N_2^T]x(s) \\
& + 2x^T(t-\tau)[- \tau M_2^T - \tau^2 2N_2^T]\dot{x}(s) \\
& + f^T(x(t))[r^2 Q_8 + S]f(x(t)) \\
& + 2f^T(x(t))h[W_0^T P_{13}]x(s) + 2f^T(x(t))\tau[W_0^T P_{14}]x(s) \\
& + 2f^T(x(t-\tau))[-S]f(x(t-\tau)) + 2f^T(x(t-\tau))h[W_1^T P_{13}]x(s) \\
& + 2f^T(x(t-\tau))\tau[W_1^T P_{14}]x(s) \\
& + 2\int_{t-r}^t f^T(x(s))ds[-Q_8]\int_{t-r}^t f(x(s))ds + \int_{t-r}^t f^T(x(s))h[W_2^T P_{13}]x(s) \\
& + 2\int_{t-r}^t f^T(x(s))ds\tau[W_2^T P_{14}]x(s) \\
& + x^T(s)[-hQ_4]x(s) + x^T(s)[- \tau Q_5]x(s) \\
& + \dot{x}^T(s)[-hQ_6]\dot{x}(s) + \dot{x}^T(s)[- \tau Q_7]\dot{x}(s)
\end{aligned}$$

$$+ \dot{x}^T(t)[hQ_6 + \tau Q_7 + Q_2]\dot{x}(t). \tag{16}$$

Then  $\dot{x}^T(t)[hQ_6 + \tau Q_7 + Q_2]\dot{x}(t) = 0$ , sub into (19),

$$\dot{V}(t, x) \leq \eta^T(t) \Xi^1 \eta(t) + \eta^T(t) \Xi^2 \eta(t). \tag{17}$$

$$\dot{V}(t, x) \leq 0, \tag{18}$$

Where

$$\eta = \left[ x^T(t) \ x^T(t-h) \ \dot{x}^T(t-h) \ x^T(t-\tau) \ f^T(x(t)) \ f^T(x(t-\tau)) \int_{t-r}^t f(x(s))ds \ x^T(s) \ \dot{x}^T(s) \right]^T$$

and thus according to Lyapunov stability theory, The nominal system (1) is asymptotically stable.

$$P_{11} = 10^{-6} \begin{bmatrix} 0.0466 & -0.1564 \\ -0.1564 & 1.0949 \end{bmatrix},$$

#### IV. NUMERICAL EXAMPLE

To illustrate the usefulness of the proposed approach, we present the following example.

$$P_{12} = 10^{-6} \begin{bmatrix} 0.0333 & -0.0595 \\ -0.0595 & 0.0542 \end{bmatrix},$$

Consider the following uncertain Neutral-type systems with the parameters as follows:

$$P_{13} = 10^{-6} \begin{bmatrix} 0.1476 & -0.0014 \\ -0.0014 & 0.1363 \end{bmatrix},$$

$$\dot{x}(t) = -Ax(t) + W_0 f(x(t)) + W_1 f(x(t-\tau)) + C\dot{x}(t-h) + W_2 \int_{t-r}^t f(x(s))ds$$

$$P_{14} = 10^{-6} \begin{bmatrix} 0.1562 & -0.0500 \\ -0.0500 & 1.8133 \end{bmatrix},$$

$$A = \begin{bmatrix} -0.05 & 0 \\ 0 & -1.8 \end{bmatrix}, \quad W_0 = \begin{bmatrix} -0.02 & 0 \\ -0.05 & 1 \end{bmatrix},$$

$$P_{22} = 10^{-6} \begin{bmatrix} 0.2785 & -0.3741 \\ -0.3741 & 0.3.2018 \end{bmatrix},$$

$$W_1 = \begin{bmatrix} 4 & 0.1 \\ 0.2 & -0.03 \end{bmatrix}, \quad W_2 = \begin{bmatrix} -6.5 & 1 \\ 0.2 & 0.1 \end{bmatrix},$$

$$P_{23} = \begin{bmatrix} -0.1477 & -0.0004 \\ -0.0004 & -0.1440 \end{bmatrix}$$

$$C = \begin{bmatrix} -1 & 1 \\ 0.2 & 0.1 \end{bmatrix}, \quad D = \begin{bmatrix} 0.2 & 0 \\ 0 & 0.2 \end{bmatrix},$$

$$P_{24} = 10^{-6} \begin{bmatrix} 5.4204 & -0.1904 \\ -0.1904 & 5.7305 \end{bmatrix},$$

$$E_1 = \begin{bmatrix} 0.5 & 0 \\ 0 & 0.5 \end{bmatrix}, \quad E_3 = \begin{bmatrix} 0.5 & 0 \\ 0 & 0.5 \end{bmatrix},$$

$$P_{33} = 10^{-6} \begin{bmatrix} 0.3873 & -0.1851 \\ -0.1851 & 3.8283 \end{bmatrix}$$

$$E_4 = \begin{bmatrix} 0.5 & 0 \\ 0 & 0.5 \end{bmatrix}$$

$$P_{34} = 10^{-6} \begin{bmatrix} 0.7163 & -0.7828 \\ -0.7828 & 9.9407 \end{bmatrix},$$

$$E_5 = \begin{bmatrix} 0.5 & 0 \\ 0 & 0.5 \end{bmatrix}, \quad E_6 = \begin{bmatrix} 0.5 & 0 \\ 0 & 0.5 \end{bmatrix},$$

$$P_{44} = 10^{-6} \begin{bmatrix} 4.1666 & 0 \\ 0 & 4.1666 \end{bmatrix}$$

with  $\varepsilon = 0.35, h = 0.01, \tau = 0.02, r = 0.01$ . Then by applying Theorem 3.1 in MATLAB LMI Toolbox the feasible solutions are

$$Q_1 = 10^{-6} \begin{bmatrix} 6.3798 & -0.0489 \\ -0.0489 & 5.7799 \end{bmatrix},$$

$$Q_2 = \begin{bmatrix} 0.0030 & -0.0023 \\ -0.0023 & 0.0074 \end{bmatrix},$$

$$Q_3 = 10^{-6} \begin{bmatrix} 1.4845 & 0.0155 \\ 0.0155 & 1.5291 \end{bmatrix},$$

$$Q_4 = \begin{bmatrix} 0.0138 & 0.0022 \\ 0.0022 & 0.0090 \end{bmatrix},$$

$$Q_5 = 10^{-6} \begin{bmatrix} 4.0398 & 0.0070 \\ 0.0070 & 4.0488 \end{bmatrix},$$

$$Q_6 = \begin{bmatrix} 0.0040 & -0.0433 \\ -0.0433 & 0.4208 \end{bmatrix}$$

$$Q_7 = \begin{bmatrix} 0.1262 & -0.9209 \\ -0.9209 & 7.0205 \end{bmatrix},$$

$$Q_8 = \begin{bmatrix} 5.2884 & 0.0101 \\ 0.0101 & 6.8036 \end{bmatrix}$$

Therefore the uncertain Neutral-type systems is asymptotically stable.

#### CONCLUSION

In this paper, by constructing an appropriate Lyapunov-Krasovskii functional, and employing the free-weighting matrices technique, some sufficient conditions ensuring the robustly stability for uncertain neutral-type systems are derived, Numerical examples are provided to illustrate the effectiveness of our obtained results.

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